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Wayne L. Winston: Mathletics

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	N	O
2		EXP
3		2
4	Variation of MAD as Exp changes	
5		MAD
6	Exp	0.0197
7	1.0	0.0318
8	1.1	0.0297
9	1.2	0.0277
10	1.3	0.0259
11	1.4	0.0243
12	1.5	0.0228
13	1.6	0.0216
14	1.7	0.0206
15	1.8	0.0200
16	1.9	0.0196
17	2.0	0.0197
18	2.1	0.0200
19	2.2	0.0207
20	2.3	0.0216
21	2.4	0.0228
22	2.5	0.0243
23	2.6	0.0260
24	2.7	0.0278
25	2.8	0.0298
26	2.9	0.0318
27	3.0	0.0339

Figure 1.2. Dependence of Pythagorean Theorem accuracy on exponent. See file Standings.xls.

How Well Does the Pythagorean Theorem Forecast?

To test the utility of the Pythagorean Theorem (or any prediction model), we should check how well it forecasts the future. I compared the Pythagorean Theorem’s forecast for each MLB playoff series (1980–2007) against a prediction based just on games won. For each playoff series the Pythagorean method would predict the winner to be the team with the higher scoring ratio, while the “games won” approach simply predicts the winner of a playoff series to be the team that won more games. We found that the Pythagorean approach correctly predicted 57 of 106 playoff series (53.8%) while the “games won” approach correctly predicted the winner of only 50% (50 out of 100) of playoff series.³ The reader is prob-

³ In six playoff series the opposing teams had identical win-loss records so the “Games Won” approach could not make a prediction.

ably disappointed that even the Pythagorean method only correctly forecasts the outcome of less than 54% of baseball playoff series. I believe that the regular season is a relatively poor predictor of the playoffs in baseball because a team's regular season record depends greatly on the performance of five starting pitchers. During the playoffs teams only use three or four starting pitchers, so much of the regular season data (games involving the fourth and fifth starting pitchers) are not relevant for predicting the outcome of the playoffs.

For anecdotal evidence of how the Pythagorean Theorem forecasts the future performance of a team better than a team's win-loss record, consider the case of the 2005 Washington Nationals. On July 4, 2005, the Nationals were in first place with a record of 50–32. If we extrapolate this winning percentage we would have predicted a final record of 99–63. On July 4, 2005, the Nationals scoring ratio was .991. On July 4, 2005, (1)' would have predicted a final record of 80–82. Sure enough, the poor Nationals finished 81–81.

The Importance of the Pythagorean Theorem

Baseball's Pythagorean Theorem is also important because it allows us to determine how many extra wins (or losses) will result from a trade. Suppose a team has scored 850 runs during a season and has given up 800 runs. Suppose we trade a shortstop (Joe) who "created"⁴ 150 runs for a shortstop (Greg) who created 170 runs in the same number of plate appearances. This trade will cause the team (all other things being equal) to score 20 more runs

($170 - 150 = 20$). Before the trade, $R = \frac{850}{800} = 1.0625$, and we would

predict the team to have won $\frac{162(1.0625)^2}{1+(1.0625)^2} = 85.9$ games. After the

trade, $R = \frac{870}{800} = 1.0875$, and we would predict the team to win

$\frac{162(1.0875)^2}{1+(1.0875)^2} = 87.8$ games. Therefore, we estimate the trade makes our

team 1.9 games better ($87.8 - 85.9 = 1.9$). In chapter 9, we will see how the Pythagorean Theorem can be used to help determine fair salaries for MLB players.

⁴In chapters 2–4 we will explain in detail how to determine how many runs a hitter creates.

Football and Basketball “Pythagorean Theorems”

Does the Pythagorean Theorem hold for football and basketball? Daryl Morey, the general manager for the Houston Rockets, has shown that for the NFL, equation (2) with $\text{exp} = 2.37$ gives the most accurate predictions for winning percentage while for the NBA, equation (2) with $\text{exp} = 13.91$ gives the most accurate predictions for winning percentage. Figure 1.3 gives the predicted and actual winning percentages for the NFL for the 2006 season, while figure 1.4 gives the predicted and actual winning percentages for the NBA for the 2006–7 season.

For the 2005–7 NFL seasons, MAD was minimized by $\text{exp} = 2.7$. $\text{Exp} = 2.7$ yielded a MAD of 5.9%, while Morey’s $\text{exp} = 2.37$ yielded a MAD of 6.1%. For the 2004–7 NBA seasons, $\text{exp} = 15.4$ best fit actual winning percentages. MAD for these seasons was 3.36% for $\text{exp} = 15.4$ and 3.40% for $\text{exp} = 13.91$. Since Morey’s values of exp are very close in accuracy to the values we found from recent seasons we will stick with Morey’s values of exp .

These predicted winning percentages are based on regular season data. Therefore, we could look at teams that performed much better than expected during the regular season and predict that “luck would catch up

	B	C	D	E	F	G	H	I	J	K	L	M	N
3			exp = 2.4						MAD = 0.061497				
4													
5	Year	Team	Wins	Losses	Points for	Points against	Ratio	Predicted winning %	Annual winning %	abserr		exp	MAD
6	2007	N.E. Patriots	16	0	589	274	2.149635	0.859815262	1	0.140185			0.061497
7	2007	B. Bills	7	9	252	354	0.711864	0.308853076	0.4375	0.128647		1.5	0.08419
8	2007	N.Y. Jets	4	12	268	355	0.75493	0.339330307	0.25	0.08933		1.6	0.080449
9	2007	M.Dolphins	1	15	267	437	0.610984	0.237277785	0.625	0.174778		1.7	0.077006
10	2007	C. Browns	10	6	402	382	1.052356	0.530199349	0.625	0.094801		1.8	0.073795
11	2007	P. Steelers	10	6	393	269	1.460967	0.710633507	0.625	0.085634		1.9	0.070675
12	2007	C. Bengals	7	9	380	385	0.987013	0.492255411	0.4375	0.054755		2	0.068155
13	2007	B. Ravens	5	11	275	384	0.716146	0.311894893	0.3125	0.000605		2.1	0.06588
14	2007	I. Colts	13	3	450	262	1.717557	0.782779877	0.8125	0.02972		2.2	0.064002
15	2007	J. Jaguars	11	5	411	304	1.351974	0.67144112	0.6875	0.016059		2.3	0.062394
16	2007	T. Titans	10	6	301	297	1.013468	0.507925876	0.625	0.117074		2.4	0.061216
17	2007	H. Texans	8	8	379	384	0.986979	0.492235113	0.5	0.007765		2.5	0.060312
18	2007	S.D. Chargers	11	5	412	284	1.450704	0.707186057	0.6875	0.019686		2.6	0.059554
19	2007	D. Broncos	7	9	320	409	0.782396	0.35856816	0.4375	0.078932	best!	2.7	0.059456
20	2007	O. Raiders	4	12	283	398	0.711055	0.308278013	0.25	0.058278		2.8	0.059828
21	2007	K.C. Chiefs	4	12	226	335	0.674627	0.282352662	0.25	0.032353		2.9	0.060934
22	2007	D. Cowboys	13	3	455	325	1.4	0.689426435	0.8125	0.123074		3	0.062411
23	2007	N.Y. Giants	10	6	373	351	1.062678	0.535957197	0.625	0.089043		3.4	0.063891

Figure 1.3. Predicted NFL winning percentages. $\text{Exp} = 2.4$. See file Sportshw1.xls.

	E	F	G	H	I	J	K
37	2006–2007 NBA						MAD = 0.05
38							
39	Team	PF	PA	Ratio	Predicted Win %	Actual Win %	Abs. Error
40	Phoenix Suns	110.2	102.9	1.07	0.722	0.744	0.022
41	Golden State Warriors	106.5	106.9	1.00	0.487	0.512	0.025
42	Denver Nuggets	105.4	103.7	1.02	0.556	0.549	0.008
43	Washington Wizards	104.3	104.9	0.99	0.480	0.500	0.020
44	L.A. Lakers	103.3	103.4	1.00	0.497	0.512	0.016
45	Memphis Grizzlies	101.6	106.7	0.95	0.336	0.268	0.068
46	Utah Jazz	101.5	98.6	1.03	0.599	0.622	0.022
47	Sacramento Kings	101.3	103.1	0.98	0.439	0.395	0.044
48	Dallas Mavericks	100	92.8	1.08	0.739	0.817	0.078
49	Milwaukee Bucks	99.7	104	0.96	0.357	0.341	0.016
50	Toronto Raptors	99.5	98.5	1.01	0.535	0.573	0.038
51	Seattle Superonics	99.1	102	0.97	0.401	0.378	0.023
52	Chicago Bulls	98.8	93.8	1.05	0.673	0.598	0.076
53	San Antonio Spurs	98.5	90.1	1.09	0.776	0.707	0.068
54	New Jersey Nets	97.6	98.3	0.99	0.475	0.500	0.025
55	New York Knicks	97.5	100.3	0.97	0.403	0.402	0.000
56	Houston Rockets	97	92.1	1.05	0.673	0.634	0.039
57	Charlotte Bobcats	96.9	100.6	0.96	0.373	0.402	0.030
58	Cleveland Cavaliers	96.8	92.9	1.04	0.639	0.610	0.029
59	Minnesota Timberwolves	96.1	99.7	0.96	0.375	0.395	0.020
60	Detroit Pistons	96	91.8	1.05	0.651	0.646	0.004
61	Boston Celtics	95.8	99.2	0.97	0.381	0.293	0.088
62	Indiana Pacers	95.6	98	0.98	0.415	0.427	0.012
63	L.A. Clippers	95.6	96.1	0.99	0.482	0.952	0.471
64	New Orleans Hornets	95.5	97.1	0.98	0.442	0.476	0.033
65	Philadelphia 76ers	94.9	98	0.97	0.390	0.427	0.037
66	Orlando Magic	94.8	94	1.01	0.529	0.488	0.042
67	Miami Heat	94.6	95.5	0.99	0.467	0.537	0.069
68	Portland Trail Blazers	94.1	98.4	0.96	0.349	0.390	0.041
69	Atlanta Hawks	93.7	98.4	0.95	0.336	0.366	0.030

Figure 1.4. Predicted NBA winning percentages. $Exp = 13.91$. See file Footballbasketballpythagoras.xls.

with them.” This train of thought would lead us to believe that these teams would perform worse during the playoffs. Note that the Miami Heat and Dallas Mavericks both won about 8% more games than expected during the regular season. Therefore, we would have predicted Miami and Dallas to perform worse during the playoffs than their actual win-loss record indicated. Sure enough, both Dallas and Miami suffered unexpected first-round defeats. Conversely, during the regular season the San Antonio Spurs and Chicago Bulls won around 8% fewer games than the Pythagorean Theorem predicts, indicating that these teams would perform better than expected in the playoffs. Sure enough, the Bulls upset the Heat and gave the Detroit Pistons a tough time. Of course, the Spurs won the 2007 NBA title. In addition, the Pythagorean Theorem had the Spurs as by far the league’s best team (78% predicted winning percentage). Note the team that under-achieved the most was the Boston Celtics, who won nearly 9% fewer (or 7)

games than predicted. Many people suggested the Celtics “tanked” games during the regular season to improve their chances of obtaining potential future superstars such as Greg Oden and Kevin Durant in the 2007 draft lottery. The fact that the Celtics won seven fewer games than expected does not prove this conjecture, but it is certainly consistent with the view that Celtics did not go all out to win every close game.

APPENDIX

Data Tables

The Excel Data Table feature enables us to see how a formula changes as the values of one or two cells in a spreadsheet are modified. This appendix shows how to use a One Way Data Table to determine how the accuracy of (2) for predicting team winning percentage depends on the value of exp . To illustrate, let’s show how to use a One Way Data Table to determine how varying exp from 1 to 3 changes the average error in predicting a MLB team’s winning percentage (see figure 1.2).

Step 1. We begin by entering the possible values of exp (1, 1.1, . . . 3) in the cell range N7:N27. To enter these values, simply enter 1 in N7, 1.1 in N8, and select the cell range N8. Now drag the cross in the lower right-hand corner of N8 down to N27.

Step 2. In cell O6 we enter the formula we want to loop through and calculate for different values of exp by entering the formula = J1.

Step 3. In Excel 2003 or earlier, select Table from the Data Menu. In Excel 2007 select Data Table from the What If portion of the ribbon’s Data tab (figure 1-a).

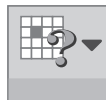


Figure 1-a. What If icon for Excel 2007.

Step 4. Do not select a row input cell but select cell L2 (which contains the value of exp) as the column input cell. After selecting OK we see the results shown in figure 1.2. In effect Excel has placed the values 1, 1.1, . . . 3 into cell M2 and computed our MAD for each listed value of exp .